

CBSE Class 10 Mathematics - 02
Solved Sample / Practice Paper - 2025-26
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Time Allowed: 3 hours

Maximum Marks: 80 (Theory)

Language: English

Calculator: Not allowed

General Instructions:

1. All questions are compulsory.
2. The paper contains five sections: A, B, C, D, and E.
3. Section A has 20 multiple-choice questions (MCQs) carrying 1 mark each.
4. Section B has 5 short answer-I (SA-I) type questions carrying 2 marks each.
5. Section C has 6 short answer-II (SA-II) type questions carrying 3 marks each.
6. Section D has 4 long answer (LA) type questions carrying 5 marks each.
7. Section E has 3 case based integrated units of assessment (4 marks each) with sub-parts of the values of 1, 1 and 2 marks each respectively.
8. All questions are compulsory. However, an internal choice in 2 questions of 5 marks, 2 questions of 3 marks and 2 questions of 2 marks has been provided. An internal choice has been provided in the 2 marks questions of Section E.
9. Draw neat figures wherever required. Take $\pi = 22/7$ wherever required if not stated.

Section A (20 × 1 = 20 marks)

1. The prime factorization of 156 is:
a) $2 \times 3 \times 13$
b) $2^2 \times 3 \times 13$
c) $2 \times 3^2 \times 13$
d) $2^2 \times 3^2 \times 13$
2. If one zero of the quadratic polynomial $x^2 + 3x + k$ is 2, then the value of k is:
a) 10
b) -10

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- c) 5
d) -5
3. The lines represented by the equations $6x-3y+10=0$ and $2x-y+9=0$ are:
a) Intersecting at exactly one point
b) Parallel
c) Coincident
d) Intersecting at exactly two points
4. The discriminant of the quadratic equation $2x^2-4x+3=0$ is:
a) 8
b) -8
c) 40
d) -40
5. Which term of the AP: 21, 18, 15, ... is -81?
a) 33rd
b) 34th
c) 35th
d) 36th
6. The point which divides the line segment joining the points A(7, -6) and B(3, 4) in the ratio 1:2 internally lies in the:
a) I quadrant
b) II quadrant
c) III quadrant
d) IV quadrant
7. In triangle ABC, right-angled at B, if $\sin A = \frac{3}{5}$, then the value of $\cos A$ is:
a) $\frac{4}{5}$
b) $\frac{3}{4}$
c) $\frac{5}{4}$
d) $\frac{5}{3}$
8. The value of $(1+\tan^2 A)/(1+\cot^2 A)$ is:
a) $\sec^2 A$
b) -1
c) $\cot^2 A$
d) $\tan^2 A$
9. From a point Q, the length of the tangent to a circle is 24 cm and the distance of Q from the centre is 25 cm. The radius of the circle is:
a) 7 cm
b) 12 cm
c) 15 cm
d) 24.5 cm
10. If triangle ABC ~ triangle PQR, $\text{area}(\text{triangle ABC}) = 81 \text{ cm}^2$, and $\text{area}(\text{triangle PQR}) = 121 \text{ cm}^2$. If $QR = 15.4 \text{ cm}$, then BC equals:
a) 12.6 cm
b) 13.1 cm
c) 14.2 cm
d) 11.2 cm

11. The area of the sector of a circle with radius 6 cm if the angle of the sector is 60° is:
a) $132/7 \text{ cm}^2$
b) $142/7 \text{ cm}^2$
c) $152/7 \text{ cm}^2$
d) $122/7 \text{ cm}^2$
12. A metallic sphere of radius 4.2 cm is melted and recast into the shape of a cylinder of radius 6 cm. The height of the cylinder is:
a) 2.74 cm
b) 3.74 cm
c) 4.74 cm
d) 5.74 cm
13. The cumulative frequency curve is also called:
a) Histogram
b) Ogive
c) Bar graph
d) Pictograph
14. Two dice are thrown together. The probability of getting a doublet is:
a) $1/3$
b) $1/6$
c) $1/2$
d) $1/4$
15. If $2\sin(2\theta) = \sqrt{3}$, then the value of θ is:
a) 15°
b) 30°
c) 45°
d) 60°
16. The top of two poles of height 20 m and 14 m are connected by a wire. If the wire makes an angle of 30° with the horizontal, then the length of the wire is:
a) 10 m
b) 12 m
c) 14 m
d) 8 m
17. The HCF of two numbers is 18 and their product is 12960. Their LCM will be:
a) 420
b) 600
c) 720
d) 800
18. A quadratic polynomial, whose zeroes are -3 and 4, is:
a) $x^2 - x + 12$
b) $x^2 + x + 12$
c) $x^2 - x - 12$
d) $2x^2 + 2x - 24$
19. Assertion (A): The sum of the first 'n' terms of an AP is given by $S_n = 3n^2 - 4n$. The common difference of the AP is 6.
Reason (R): The common difference of an AP can be found by $d = a_2 - a_1$.

- a) Both A and R are true and R is the correct explanation of A.
 b) Both A and R are true but R is not the correct explanation of A.
 c) A is true but R is false.
 d) A is false but R is true.
20. Assertion (A): In a circle of radius 6 cm, the angle of a sector is 60° . Then the area of the sector is $132/7 \text{ cm}^2$.
 Reason (R): Area of a sector of a circle with radius r and angle θ is given by $(\theta/360) \times \pi r^2$.
 a) Both A and R are true and R is the correct explanation of A.
 b) Both A and R are true but R is not the correct explanation of A.
 c) A is true but R is false.
 d) A is false but R is true.

Section B ($5 \times 2 = 10$ marks)

21. Find the value of k for which the quadratic equation $kx(x-2)+6=0$ has two equal roots.
 22. Find the ratio in which the y -axis divides the line segment joining the points $(5, -6)$ and $(-1, -4)$.
 23. Two tangents TP and TQ are drawn to a circle with centre O from an external point T. Prove that $\angle PTQ = 2\angle OPQ$.
 24. A bag contains 3 red balls and 5 black balls. A ball is drawn at random from the bag. What is the probability that the ball drawn is (i) red? (ii) not red?
 25. In triangle PQR, right-angled at Q, $PR + QR = 25 \text{ cm}$ and $PQ = 5 \text{ cm}$. Determine the value of $\sin P$.
OR
 If $\tan A = 3/4$, find the value of $1/\sin A + 1/\cos A$.

Section C ($6 \times 3 = 18$ marks)

26. Prove that $3+2\sqrt{5}$ is irrational.
 27. If α and β are the zeroes of the quadratic polynomial $f(x) = x^2 - 5x + 4$, find the value of $1/\alpha + 1/\beta - 2\alpha\beta$.
 28. A fraction becomes $1/3$ when 1 is subtracted from the numerator and it becomes $1/4$ when 8 is added to its denominator. Find the fraction.
OR
 The sum of a two-digit number and the number obtained by reversing the digits is 66. If the digits of the number differ by 2, find the number.
 29. Prove that the parallelogram circumscribing a circle is a rhombus.
 30. Prove that: $(\operatorname{cosec} \theta - \cot \theta)^2 = (1 - \cos \theta)/(1 + \cos \theta)$.
OR
 If $\sin(A-B) = 1/2$, $\cos(A+B) = 1/2$, $0^\circ < A+B \leq 90^\circ$, find A and B .
 31. A die is thrown twice. What is the probability that
 (i) 5 will not come up either time?

- (ii) 5 will come up at least once?
 (iii) the sum of the numbers is 8?

Section D ($4 \times 5 = 20$ marks)

32. An express train takes 1 hour less than a passenger train to travel 132 km between Mysuru and Bengaluru. If the average speed of the express train is 11 km/h more than that of the passenger train, find the average speed of the two trains.

OR

The diagonal of a rectangular field is 60 metres more than the shorter side. If the longer side is 30 metres more than the shorter side, find the sides of the field.

33. State and prove the Pythagoras Theorem.
 34. A toy is in the form of a cone of radius 3.5 cm mounted on a hemisphere of the same radius. The total height of the toy is 15.5 cm. Find the total surface area of the toy.

OR

A well of diameter 3 m is dug 14 m deep. The earth taken out of it has been spread evenly all around it in the shape of a circular ring of width 4 m to form an embankment. Find the height of the embankment.

35. The distribution below gives the weights of 30 students of a class. Find the median weight of the students.

Weight (in kg)	40-45	45-50	50-55	55-60	60-65	65-70	70-75
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Number of students	2	3	8	6	6	3	2

Section E ($3 \times 4 = 12$ marks)

36. Case Study 1: Parabolic Arch

The arch of a bridge is in the shape of a parabola. The arch is 8m high at the center and 32m wide at the base. The parabolic shape can be represented by a quadratic polynomial. Consider the base of the arch to be along the x-axis with the vertex at (0, 8).

(A diagram showing a parabolic arch with vertex at (0,8) and base on the x-axis, spanning from $x=-16$ to $x=16$.)

- (i) What are the zeroes of the polynomial that represents the arch? (1)
 (ii) Find the quadratic polynomial that represents the arch. (1)
 (iii) What is the height of the arch at a distance of 8m from the center? (2)

OR

(iii) The highway over the bridge has two lanes of 4m width each. How much width of the arch is over the highway? (2)

37. Case Study 2: Gardening

A group of students of class 10 were selected for a school gardening project. They planted saplings in a triangular plot of land. The vertices of the triangular plot are P(0, 4), Q(3, 1), and R(3, 7).

(A coordinate plane showing a triangle with vertices P(0,4), Q(3,1), and R(3,7).)

- (i) Find the distance between the vertices P and Q. (1)
- (ii) Find the coordinates of the centroid of the triangle PQR. (1)
- (iii) Find the area of the triangular plot PQR. (2)

OR

- (iii) Determine the type of triangle PQR based on its side lengths. (2)

38. Case Study 3: School Fete

A committee for a school fete is selling raffle tickets. They have 250 tickets in total. Out of these, one ticket will win the first prize (a laptop), 5 tickets will win the second prize (a tablet), and 20 tickets will win the third prize (a power bank). The rest of the tickets do not win any prize. A ticket is drawn at random.

- (i) What is the probability that the ticket drawn wins the first prize? (1)
- (ii) What is the probability that the ticket drawn wins any prize? (1)
- (iii) What is the probability that the ticket drawn wins either the second or third prize? (2)

Answer Key (for Section A)

Q.No.	Answer
1	b
2	b
3	b
4	b
5	c



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6	d
7	a
8	d
9	a
10	a
11	a
12	a
13	b
14	b
15	b
16	b



17	c
18	c
19	a
20	a

Detailed Marking Scheme & Fully Worked Solutions

Section A

- Solution:** (b) $22 \times 3 \times 13 = 156 = 2 \times 78 = 2 \times 2 \times 39 = 22 \times 3 \times 13$. **(1 mark)**
- Solution:** (b) -10. If 2 is a zero, then $(2)^2 + 3(2) + k = 0 \Rightarrow 4 + 6 + k = 0 \Rightarrow k = -10$. **(1 mark)**
- Solution:** (b) Parallel. Here, $a_1/a_2 = 6/2 = 3$, $b_1/b_2 = -3/-1 = 3$, $c_1/c_2 = 10/9$. Since $a_1/a_2 = b_1/b_2 \neq c_1/c_2$, the lines are parallel. **(1 mark)**
- Solution:** (b) -8. $D = b^2 - 4ac = (-4)^2 - 4(2)(3) = 16 - 24 = -8$. **(1 mark)**
- Solution:** (c) 35th.
 $a_n = a + (n-1)d \Rightarrow -81 = 21 + (n-1)(-3) \Rightarrow -102 = (n-1)(-3) \Rightarrow 34 = n-1 \Rightarrow n = 35$. **(1 mark)**
- Solution:** (d) IV quadrant. Using section formula, $x = (1 \cdot 3 + 2 \cdot 7)/(1+2) = 17/3$.
 $y = (1 \cdot 4 + 2 \cdot (-6))/(1+2) = -8/3$. Point $(17/3, -8/3)$ is in IV quadrant. **(1 mark)**
- Solution:** (a) $4/5$. $\sin A = P/H = 3/5$. $B = \sqrt{H^2 - P^2} = \sqrt{5^2 - 3^2} = \sqrt{16} = 4$. $\cos A = B/H = 4/5$. **(1 mark)**
- Solution:** (d) $\tan 2A$.
 $(1 + \tan 2A)/(1 + \cot 2A) = \sec 2A / \operatorname{cosec} 2A = (1/\cos 2A)/(1/\sin 2A) = \sin 2A / \cos 2A = \tan 2A$. **(1 mark)**
- Solution:** (a) 7 cm. By Pythagoras theorem, $r = \sqrt{25^2 - 24^2} = \sqrt{(25-24)(25+24)} = \sqrt{1 \times 49} = 7$ cm. **(1 mark)**
- Solution:** (a) 12.6 cm. Ratio of areas = square of ratio of sides.
 $81/121 = (BC/QR)^2 \Rightarrow 9/11 = BC/15.4 \Rightarrow BC = (9 \times 15.4)/11 = 12.6$ cm. **(1 mark)**

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11. **Solution:** (a) $132/7 \text{ cm}^2$. Area = $(\theta/360) \times \pi r^2 = (60/360) \times \pi (22/7)^2 \times 36 = 132/7 \text{ cm}^2$. (1 mark)
12. **Solution:** (a) 2.74 cm. Volume of sphere = Volume of cylinder.
 $(4/3)\pi(4.2)^3 = \pi(6)^2 h \Rightarrow h = (4/3) \times (4.2^3 \times 3) / 6^2 \approx 2.74 \text{ cm}$. (1 mark)
13. **Solution:** (b) Ogive. (1 mark)
14. **Solution:** (b) $1/6$. Doublets are (1,1), (2,2), ..., (6,6). Total 6 outcomes. Total possible outcomes = 36. $P(\text{doublet}) = 6/36 = 1/6$. (1 mark)
15. **Solution:** (b) 30° . $\sin(2\theta) = \sqrt{3}/2 = \sin(60^\circ) \Rightarrow 2\theta = 60^\circ \Rightarrow \theta = 30^\circ$. (1 mark)
16. **Solution:** (b) 12 m. Height difference = $20 - 14 = 6 \text{ m}$. Let L be the length of wire.
 $\sin 30^\circ = 6/L \Rightarrow 1/2 = 6/L \Rightarrow L = 12 \text{ m}$. (1 mark)
17. **Solution:** (c) 720. $\text{HCF} \times \text{LCM} = \text{Product of numbers}$.
 $18 \times \text{LCM} = 12960 \Rightarrow \text{LCM} = 12960/18 = 720$. (1 mark)
18. **Solution:** (c) $x^2 - x - 12$. Polynomial is $k(x^2 - (\text{sum of zeroes})x + (\text{product of zeroes}))$. Sum = $-3 + 4 = 1$. Product = -12 . For $k=1$, $x^2 - x - 12$. (1 mark)
19. **Solution:** (a) Both A and R are true and R is the correct explanation of A.
 $S_1 = a_1 = 3(1)^2 - 4(1) = -1$. $S_2 = 3(2)^2 - 4(2) = 12 - 8 = 4$. $a_2 = S_2 - S_1 = 4 - (-1) = 5$.
 $d = a_2 - a_1 = 5 - (-1) = 6$. A is true. R is the definition used to find d, hence correct explanation. (1 mark)
20. **Solution:** (a) Both A and R are true and R is the correct explanation of A. Area = $(60/360) \times \pi (22/7)^2 \times 36 = 132/7 \text{ cm}^2$. R provides the formula used in A. (1 mark)

Section B

21. **Solution:** The equation is $kx^2 - 2kx + 6 = 0$. For equal roots, $D = 0$. (1/2 mark).
 $(-2k)^2 - 4(k)(6) = 0 \Rightarrow 4k^2 - 24k = 0$. (1 mark). $4k(k-6) = 0$. Since k cannot be 0 (for a quadratic equation), $k = 6$. (1/2 mark)
22. **Solution:** Let the ratio be $k:1$. The point on the y-axis is (0, y). (1/2 mark). The x-coordinate is $0 = (k(-1) + 1(5))/(k+1) \Rightarrow -k + 5 = 0 \Rightarrow k = 5$. (1 mark). The ratio is 5:1. (1/2 mark)
23. **Solution:** Let $\angle OPQ = \theta$. In $\triangle OPQ$, $OP = OQ$ (radii), so $\angle OQP = \theta$.
 $\angle POQ = 180^\circ - 2\theta$. (1/2 mark). In quadrilateral $TPOQ$, $\angle TPO = \angle TQO = 90^\circ$. So,
 $\angle PTQ + \angle POQ = 180^\circ$. (1 mark). $\angle PTQ = 180^\circ - (180^\circ - 2\theta) = 2\theta = 2\angle OPQ$.
Hence proved. (1/2 mark)
24. **Solution:** Total balls = $3 + 5 = 8$.
(i) $P(\text{red}) = \text{Number of red balls} / \text{Total balls} = 3/8$. (1 mark)
(ii) $P(\text{not red}) = 1 - P(\text{red}) = 1 - 3/8 = 5/8$. (1 mark)
25. **Solution:** Given $PR + QR = 25$ and $PQ = 5$. Let $QR = x$, then $PR = 25 - x$.
In right $\triangle PQR$, $PR^2 = PQ^2 + QR^2 \Rightarrow (25-x)^2 = 5^2 + x^2$. (1 mark)
 $625 - 50x + x^2 = 25 + x^2 \Rightarrow 600 = 50x \Rightarrow x = 12$.
So, $QR = 12 \text{ cm}$, $PR = 13 \text{ cm}$. $\sin P = QR/PR = 12/13$. (1 mark)
- OR**
- Solution:** $\tan A = P/B = 3/4$. Hypotenuse $H = \sqrt{3^2 + 4^2} = 5$. (1/2 mark)
 $\sin A = 3/5$, $\cos A = 4/5$. (1/2 mark)
 $1/\sin A + 1/\cos A = 5/3 + 5/4 = (20+15)/12 = 35/12$. (1 mark)

Section C

26. Solution: Let us assume, to the contrary, that $3+2\sqrt{5}$ is rational. So, $3+2\sqrt{5}=a/b$, where a and b are coprime integers, $b \neq 0$. (1/2 mark)
 $2\sqrt{5}=a/b-3=(a-3b)/b$. (1 mark)
 $\sqrt{5}=(a-3b)/(2b)$. (1/2 mark)
 Since a and b are integers, $(a-3b)/(2b)$ is rational, and so $\sqrt{5}$ is rational. But this contradicts the fact that $\sqrt{5}$ is irrational. (1 mark)
 This contradiction arises from our incorrect assumption. Thus, $3+2\sqrt{5}$ is irrational.
27. Solution: For x^2-5x+4 , we have $\alpha+\beta=-(-5)/1=5$ and $\alpha\beta=4/1=4$. (1 mark)
 We need to find $1/\alpha+1/\beta-2\alpha\beta$.
 $1/\alpha+1/\beta=(\alpha+\beta)/(\alpha\beta)=5/4$. (1 mark)
 So, the value is $5/4-2(4)=5/4-8=(5-32)/4=-27/4$. (1 mark)
28. Solution: Let the fraction be x/y .
 $(x-1)/y=1/3 \Rightarrow 3x-3=y \Rightarrow 3x-y=3$... (i) (1 mark)
 $x/(y+8)=1/4 \Rightarrow 4x=y+8 \Rightarrow 4x-y=8$... (ii) (1 mark)
 Subtracting (i) from (ii), we get $x=5$.
 From (i), $y=3(5)-3=12$. The fraction is $5/12$. (1 mark)
- OR**
- Solution: Let the digits be x and y . Number = $10x + y$. Reversed number = $10y + x$.
 Given $(10x+y)+(10y+x)=66 \Rightarrow 11x+11y=66 \Rightarrow x+y=6$... (i) (1 mark)
 Also, $|x-y|=2 \Rightarrow x-y=2$ or $y-x=2$. (1 mark)
 Case 1: $x-y=2$. Solving with (i), we get $2x=8 \Rightarrow x=4, y=2$. Number is 42.
 Case 2: $y-x=2$. Solving with (i), we get $2y=8 \Rightarrow y=4, x=2$. Number is 24.
 The number is either 42 or 24. (1 mark)
29. Solution: Let ABCD be a parallelogram circumscribing a circle.
 We know that $AB + CD = AD + BC$ (from property of circumscribing quadrilateral). (1 mark)
 Since ABCD is a parallelogram, $AB = CD$ and $AD = BC$. (1 mark)
 Substituting these in the property, we get $AB+AB=AD+AD \Rightarrow 2AB=2AD \Rightarrow AB=AD$.
 Since adjacent sides are equal, the parallelogram is a rhombus. Hence proved. (1 mark)
30. Solution: LHS = $(\operatorname{cosec}\theta - \cot\theta)^2 = (1/\sin\theta - \cos\theta/\sin\theta)^2 = ((1-\cos\theta)/\sin\theta)^2$. (1 mark)
 $= (1-\cos\theta)^2/\sin^2\theta = (1-\cos\theta)^2/(1-\cos^2\theta)$. (1 mark)
 $= (1-\cos\theta)^2/((1-\cos\theta)(1+\cos\theta)) = (1-\cos\theta)/(1+\cos\theta) = \text{RHS}$. (1 mark)
- OR**
- Solution: $\sin(A-B)=1/2 \Rightarrow A-B=30^\circ$... (i) (1 mark)
 $\cos(A+B)=1/2 \Rightarrow A+B=60^\circ$... (ii) (1 mark)
 Adding (i) and (ii), $2A=90^\circ \Rightarrow A=45^\circ$.
 Substituting in (ii), $45^\circ+B=60^\circ \Rightarrow B=15^\circ$. (1 mark)
31. Solution: Total outcomes = $6 \times 6 = 36$.
 (i) Favorable outcomes for '5 will not come up' are 5 outcomes for each die (1,2,3,4,6). So, $5 \times 5 = 25$ outcomes. $P(5 \text{ will not come up}) = 25/36$. (1 mark)
 (ii) $P(5 \text{ will come up at least once}) = 1 - P(5 \text{ will not come up either time}) = 1 - 25/36 = 11/36$. (1 mark)
 (iii) Sum is 8: (2,6), (3,5), (4,4), (5,3), (6,2). Total 5 outcomes. $P(\text{sum is 8}) = 5/36$. (1 mark)

Section D

32. Solution: Let the speed of the passenger train be x km/h. Speed of express train = $(x+11)$ km/h. (1/2 mark)

Time by passenger train = $132/x$. Time by express train = $132/(x+11)$. (1/2 mark)

According to question, $132/x - 132/(x+11) = 1$. (1 mark)

$132(x+11-x)/(x(x+11)) = 1 \Rightarrow 132 \times 11 = x^2 + 11x$.

$x^2 + 11x - 1452 = 0$. (1 mark)

$x^2 + 44x - 33x - 1452 = 0 \Rightarrow x(x+44) - 33(x+44) = 0$.

$(x-33)(x+44) = 0$. Since speed cannot be negative, $x = 33$. (1 mark)

Speed of passenger train = 33 km/h. Speed of express train = 44 km/h. (1 mark)

OR

Solution: Let the shorter side be x m. Longer side = $(x+30)$ m. Diagonal = $(x+60)$ m. (1 mark)

By Pythagoras theorem, $(x+60)^2 = (x+30)^2 + x^2$. (1 mark)

$x^2 + 120x + 3600 = x^2 + 60x + 900 + x^2$.

$x^2 - 60x - 2700 = 0$. (1 mark)

$x^2 - 90x + 30x - 2700 = 0 \Rightarrow x(x-90) + 30(x-90) = 0$.

$(x+30)(x-90) = 0$. Since side cannot be negative, $x = 90$. (1 mark)

Shorter side = 90 m. Longer side = 120 m. (1 mark)

33. Solution: Statement: In a right-angled triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides. (1 mark)

Given: A right-angled triangle ABC, right-angled at B. To Prove: $AC^2 = AB^2 + BC^2$. (1 mark)

Construction: Draw $BD \perp AC$. (1/2 mark)

Proof: In triangle ADB and triangle ABC, $\angle A = \angle A$ (common), $\angle ADB = \angle ABC = 90^\circ$.

So, $\triangle ADB \sim \triangle ABC$ (AA similarity). (1 mark)

Therefore, $AD/AB = AB/AC \Rightarrow AB^2 = AD \times AC$... (i)

Similarly, in triangle BDC and triangle ABC, $\triangle BDC \sim \triangle ABC$.

Therefore, $CD/BC = BC/AC \Rightarrow BC^2 = CD \times AC$... (ii) (1 mark)

Adding (i) and (ii), $AB^2 + BC^2 = AD \times AC + CD \times AC = AC(AD + CD) = AC \times AC = AC^2$.

Hence proved. (1/2 mark)

34. Solution: Radius $r = 3.5$ cm. Total height = 15.5 cm.

Height of cone, $h = 15.5 - 3.5 = 12$ cm. (1 mark)

Slant height of cone, $l = \sqrt{r^2 + h^2} = \sqrt{(3.5)^2 + 12^2} = \sqrt{12.25 + 144} = \sqrt{156.25} = 12.5$ cm. (1 mark)

TSA of toy = CSA of cone + CSA of hemisphere = $\pi rl + 2\pi r^2 = \pi r(l + 2r)$. (1 mark)

$= (22/7) \times 3.5(12.5 + 2 \times 3.5) = 22 \times 0.5(12.5 + 7) = 11 \times 19.5$. (1 mark)

$= 214.5 \text{ cm}^2$. (1 mark)

OR

Solution: Volume of earth dug = Volume of well = $\pi r^2 h = (22/7) \times (1.5)^2 \times 14 = 99 \text{ m}^3$. (2 marks)

The embankment is a cylindrical shell. Inner radius $r_1 = 1.5$ m. Outer radius $r_2 = 1.5 + 4 = 5.5$ m. (1 mark)

Volume of embankment = $\pi(r_2^2 - r_1^2)H$, where H is the height.

$99 = (22/7) \times ((5.5)^2 - (1.5)^2) \times H$. (1 mark)

$99 = (22/7) \times (5.5 - 1.5)(5.5 + 1.5) \times H = (22/7) \times 4 \times 7 \times H = 88H$.

$H = 99/88 = 9/8 = 1.125$ m. (1 mark)

35. Solution:

| Weight (in kg) | Frequency (f) | Cumulative Frequency (cf) |

|---|---|---|

| 40-45 | 2 | 2 |

| 45-50 | 3 | 5 |

| 50-55 | 8 | 13 |

| 55-60 | 6 | 19 | <-- Median Class |

| 60-65 | 6 | 25 |

| 65-70 | 3 | 28 |

| 70-75 | 2 | 30 |

(1 mark for cf table)

$N = 30$. $N/2 = 15$. The median class is 55-60. (1 mark)

$l = 55$, $N/2 = 15$, $cf = 13$, $f = 6$, $h = 5$. (1 mark)

Median = $l + [(N/2 - cf)/f] \times h = 55 + [(15 - 13)/6] \times 5$. (1 mark)

$= 55 + (2/6) \times 5 = 55 + 5/3 = 55 + 1.67 = 56.67$ kg. (1 mark)

Section E

36. Solution:

(i) The base is 32m wide, centered at the origin. So the arch touches the x-axis at $x = -16$ and $x = 16$. The zeroes are -16 and 16. (1 mark)

(ii) The polynomial is of the form $p(x) = k(x - 16)(x + 16) = k(x^2 - 256)$. The vertex is (0, 8), so $p(0) = 8$. $8 = k(0 - 256) \Rightarrow k = -8/256 = -1/32$. So, $p(x) = (-1/32)(x^2 - 256) = 8 - x^2/32$. (1 mark)

(iii) At a distance of 8m from the center, $x = 8$. Height = $p(8) = 8 - 8^2/32 = 8 - 64/32 = 8 - 2 = 6$ m. (2 marks)

OR

(iii) The highway spans from $x = -4$ to $x = 4$. The width is $4 - (-4) = 8$ m. (2 marks)

37. Solution:

(i) $PQ = \sqrt{(3-0)^2 + (1-4)^2} = \sqrt{3^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$ units. (1 mark)

(ii) Centroid = $((0+3+3)/3, (4+1+7)/3) = (6/3, 12/3) = (2, 4)$. (1 mark)

(iii) Area = $1/2 |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)|$
 $= 1/2 |0(1-7) + 3(7-4) + 3(4-1)| = 1/2 |0 + 3(3) + 3(3)| = 1/2 |18| = 9$ sq. units. (2 marks)

OR

(iii) $PQ = 3\sqrt{2}$. $QR = \sqrt{(3-3)^2 + (7-1)^2} = \sqrt{0+6^2} = 6$.

$PR = \sqrt{(3-0)^2 + (7-4)^2} = \sqrt{3^2 + 3^2} = \sqrt{18} = 3\sqrt{2}$.

Since $PQ = PR$, the triangle is an isosceles triangle. (2 marks)

38. Solution:

(i) Total tickets = 250. First prize tickets = 1. $P(\text{first prize}) = 1/250$. (1 mark)

(ii) Total prize tickets = 1 + 5 + 20 = 26. $P(\text{any prize}) = 26/250 = 13/125$. (1 mark)

(iii) Second or third prize tickets = 5 + 20 = 25. $P(\text{second or third prize}) = 25/250 = 1/10$. (2 marks)

Syllabus-to-Question Map

Q.No.	Unit	Chapter/Sub-topic	Skill
1	Number Systems	Real Numbers	Conceptual
2	Algebra	Polynomials	Conceptual
3	Algebra	Pair of Linear Equations	Conceptual
4	Algebra	Quadratic Equations	Conceptual
5	Algebra	Arithmetic Progressions	Application
6	Coordinate Geometry	Section Formula	Application
7	Trigonometry	Introduction to Trigonometry	Application
8	Trigonometry	Trigonometric Identities	Conceptual
9	Geometry	Circles	Application
10	Geometry	Triangles	Application

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11	Mensuration	Areas Related to Circles	Application
12	Mensuration	Surface Areas and Volumes	Application
13	Statistics & Probability	Statistics	Conceptual
14	Statistics & Probability	Probability	Application
15	Trigonometry	Trigonometric Ratios	Application
16	Trigonometry	Heights and Distances	Application
17	Number Systems	Real Numbers	Application
18	Algebra	Polynomials	Application
19	Algebra	Arithmetic Progressions	HOTS (Assertion-Reason)
20	Mensuration	Areas Related to Circles	HOTS (Assertion-Reason)
21	Algebra	Quadratic Equations	Application

22	Coordinate Geometry	Section Formula	Application
23	Geometry	Circles (Proofs)	HOTS (Proof)
24	Statistics & Probability	Probability	Application
25	Trigonometry	Introduction to Trigonometry	Application
26	Number Systems	Real Numbers (Proofs)	HOTS (Proof)
27	Algebra	Polynomials	Application
28	Algebra	Pair of Linear Equations	Application
29	Geometry	Circles (Proofs)	HOTS (Proof)
30	Trigonometry	Trigonometric Identities	HOTS (Proof)
31	Statistics & Probability	Probability	Application
32	Algebra	Quadratic Equations	HOTS (Application)

33	Geometry	Triangles (Theorems)	HOTS (Proof)
34	Mensuration	Surface Areas and Volumes	HOTS (Application)
35	Statistics & Probability	Statistics	Application
36	Algebra / Coordinate Geo	Polynomials	Competency-based
37	Coordinate Geometry	Distance & Area Formula	Competency-based
38	Statistics & Probability	Probability	Competency-based

Analytics Snapshot

- **Total Marks per Unit:**
 - Number Systems: 6 marks
 - Algebra: 20 marks
 - Coordinate Geometry: 6 marks
 - Geometry: 15 marks
 - Trigonometry: 12 marks
 - Mensuration: 10 marks
 - Statistics & Probability: 11 marks
- **Competency-based % of Paper:** 42.5% (34 marks / 80 marks)
 - Includes case studies (12 marks), Assertion-Reason (2 marks), and several application/HOTS questions.
- **Difficulty Distribution Achieved:**
 - Easy (approx. 30%): ~24 marks
 - Moderate (approx. 50%): ~41 marks
 - Challenging/HOTS (approx. 20%): ~15 marks

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