# TARUN CLASSES OF MATHEMATICS

## MATHEMATICS –STANDARD (041)
### Class X – 2019-2020

MAX. MARKS : 80                                                                                          DURATION : 3HOURS

**SECTION –A**

Q 1- Q 10 are multiple choice questions. Select the most appropriate answer from the given options.

1) Decimal representation of $\frac{246}{2^8 \times 5^{-3}}$ will be :

    a) Terminate after 6 decimal place     b) Terminate after 7 decimal place   c) not terminate   d) can't determined

2) Consider the data:

| Marks | Below 10 | Below 20 | Below30 | Below 40 | Below 50 | Below 60 |
|---|---|---|---|---|---|---|
| No.of Students | 3 | 12 | 27 | 57 | 75 | 80 |

    The modal class is:

    a) 10-20            b) 20-30            c) 30-40            d) 50-60

3) The largest number which divides 70 and 125, leaving remainders 5 and 8, respectively, is

    a) 13               b) 65              c) 875            d) 1750

4) The value of c for which the pair of equations cx – y = 2 and 6x – 2y = 3 will have infinitely many solutions is

    a) 3               b) – 3            c) –12           d) no value

5) If triangle ABC is right angled at C, then the value of sec (A+B) is :

    a) 0              b) 1              c) Not Defined          d) $\frac{2}{\sqrt{3}}$

6) If cot Θ = $\frac{15}{8}$ , Then $\frac{(2+2 \sin Θ)(1-\sin Θ)}{(1+\cos Θ)(2-2 \cos Θ)}$ equals to :

    a) $\frac{225}{64}$           b) $\frac{64}{225}$          c) $\frac{289}{64}$          d) $\frac{64}{289}$

7) Evaluate : $\frac{\sin^2 22 + \sin^2 68}{\cos^2 22 + \cos^2 68} + \sin^2 63° + \cos 63° \sin 27°$:

    a) 3             b) 2             c) 1            d) 0

8) If A(4, – 3), B(3, – 2) and C(2, 8) are vertices of a triangle, then the distance of it's centroid from the y-axis is :

    a) $\sqrt{10}$          b) 1             c) 3            d) $\frac{9}{2}$

9) Determine the ratio in which the line 2x + y – 4 = 0 divides the line segment the joining A(2, -2) and B(3, 7) :

    a) 2 : 9          b) 9 : 2          c) 7 : 2          d) 2 : 5

10) A line intersects the y-axis and x-axis at the points P and Q, respectively. If (2, –5) is the mid-point of PQ,

    then the coordinates of P and Q are, respectively

    a)) (0, – 5) and (2, 0)      b) (0, 10) and (– 4, 0)    c) (0, 4) and (– 10, 0)         d) (0, – 10) and (4, 0)

11) Find the value of a + b + c, such that the numbers a, 10, b, c, 31 are in A.P./

    If following numbers are in AP: a, 7, b, 23, c , then Evaluate : a – 2b + c.  (BONUS)

12) The areas of two similar triangles are 49 cm$^2$ and 64 cm$^2$ respectively. If the difference of the corresponding altitudes is 10 cm, then the lengths of altitudes …………………

13) *A hemispherical depression is cut out from one face of a cubical wooden block such that the diameter 'l' of the hemisphere is equal to the edge of the cube.  Surface area of the remaining solid………………………………*

14) Find the value of k such that polynomial x$^2$ – (k+6) x +2 (2k-1) has sum of its zeroes is equal to half of their product .

                                                  OR

    If the roots of the equation  12x$^2$ + mx +5  the ratio 3:2, then m …………..

15) Two friends were born in year of 2010. What is probability that they have the same birthday ?
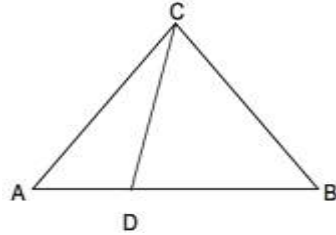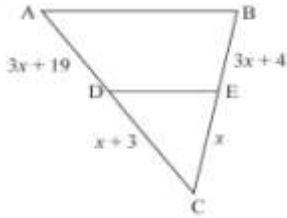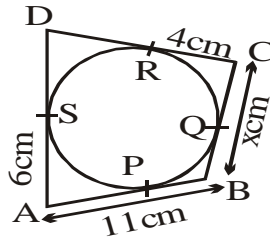
a) $\frac{1}{365}$ b) 0 c) $\frac{1}{366}$ d) 1

16) In figure, find the value of x which will make DE || AB?

In the figure, if ⦟ACB = ⦟CDA, AC = 6 cm and AD = 3 cm, then find the length of AB. (BONUS)



17) In the given figure, the circle touches the sides AB, BC, CD and DA of a quadrilateral ABCD at the points P, Q, R, S respectively. If AB = 11 cm, BC = x cm, CR = 4 cm and AS = 6 cm, find the value of x.



OR

If an angle between two tangents drawn from an external point 'P' to a circle of radius r & centre O is 60°, Find the length of OP.

18) The sum of first n terms of an A.P. is given by $(n^2 + 3n)$. Find the sum of first term & common difference.

19) What can you say about the product of rational & irrational number, justify your answer. OR

20) If -2 is a root of the quadratic equation $x^2 - px - 5 = 0$ & quadratic equation $x^2 + px + k = 0$ has equal roots, find the value of k ………………………..

## SECTION –B

21) Prove that tangent at any point of circle is perpendicular to radius through point of contact, Hence prove that If a, b, c are the sides of a right triangle where c is the hypotenuse, then prove that radius r of the circle touches the sides of the triangle is given by r = $\frac{a+b-c}{2}$.
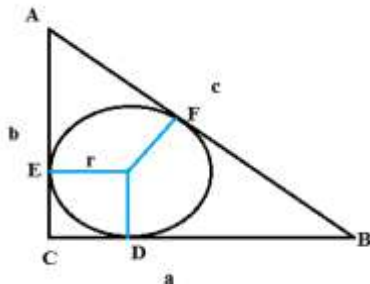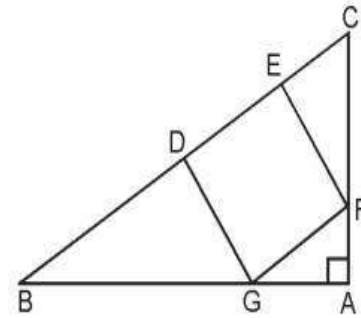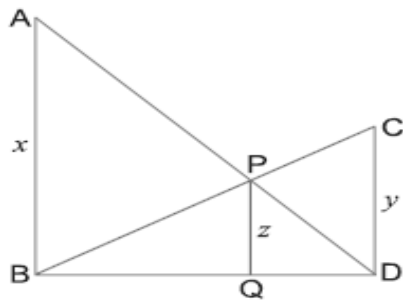
22) Find the middle term of sequence formed by all three digit numbers which leave a remainder 3 , when divided by 4.

23) In Figure , DEFG is a square & ∟BAC = 90° , Show that DE² =BD×EC .                     OR

In the given figure, it is given that ∟ABD = ∟CDB = ∟PQB = 90°. If AB = x units, CD = y units and PQ = z units, prove that

$$\frac{1}{x} + \frac{1}{y} = \frac{1}{z}.$$



24) A tower is a tall structure, taller than it is wide, often by a significant margin. Towers are distinguished from masts by their lack of guy-wires and are therefore, along with tall apartment buildings, self-supporting structures. Towers are specifically distinguished from "apartment buildings" in that they are not built to be habitable but to serve other functions.

Karan went to city and he saw a transmission tower fixed at the top of a high building. He come to know that the height of the building is 20m. From a point on the ground, the angles of elevation of the top and the bottom of a transmission tower are ⊠ and ⊠ respectively such that cos⊠ = sin(150⁰ – ⊠) and sin2⊠ = cos(135⁰ – 3⊠). Find the height of the tower.

25) Two dice are thrown together. Find the probability that :
   i)       P( a multiple of 2 on first die & a multiple of 3 on second die)
   ii)      P(the sum of the numbers on the two faces is divisible by 4 & 6 )
   iii)     P( Getting 5 only once)                                                          OR

   A bag contains white, black and red balls only. A ball is drawn at random from the bag. If the probability of getting a white ball is $\frac{3}{10}$ and that of a black ball is $\frac{2}{5}$, then find the probability of getting a red ball. If the bag contains 20 black balls, then find the total number of balls in the bag.

26) Three cubes of a metal whose edges are in the ratio 3:4:5 are melted and converted into a single cube whose diagonal is 12 √3 cm. Find the edges of the three cubes.

SECTION – C

27) Prove that product of any three consecutive integers divisible by 6 .                     **OR**

   Given that $\sqrt{5}$ is an irrational number , Prove that $3 - 2\sqrt{5}$ is an irrational number.

28) If the ratio of sum of the first m and n terms of an A.P. is $m^2 : n^2$, show that the ratio of its $m^{th}$ and $n^{th}$ terms is (2m – 1) : (2n – 1).

   If Sum of first m terms of an AP is n & sum of first n terms is m, then show that the sum of first (m + n) terms is –(m+n).(BONUS)

29)i) A boat goes 30 km upstream and 44 km downstream in 10 hours. In 13 hours, it can go 40 km upstream and 55 km down-stream. Determine the speed of the stream and that of the boat in still water.                     OR

   The area of a rectangle gets reduced by 9 square units, if its length is reduced by 5 units and breadth is increased by 3 units. If we increase the length by 3 units and the breadth by 2 units, the area increases by 67 square units. Find the dimensions of the rectangle.

   ii) Solve : $\frac{21}{x} + \frac{47}{y} = 110$ ; $\frac{47}{x} + \frac{21}{y} = 162$, x, y≠ 0.

30)Prove that : $\dfrac{\sec^3\theta}{\sec^2\theta-1} + \dfrac{\csc^3\theta}{\csc^2\theta-1} = \sec\theta\,\csc\theta(\sec\theta + \csc\theta)$                    OR

If  sec A  - tan A =  x , Show that : $\dfrac{x^2+1}{x^2-1}$ = - cosec A.

31) Find k so that $x^2 + 2x + k$ is a factor of $2x^4 + x^3 - 14\,x^2 + 5x + 6$. Also find all the zeroes of the two polynomials.

32) Sides of a right triangular field are 25m, 24m and 7m. At the three corners of the field, a cow, a buffalo and a horse are tied separately with ropes of 3.5 m each to graze in the field. Find the area of the field that cannot be grazed by these animals.

 33)        A TV reporter was given a task to prepare a report on the rainfall of the city Dispur of India in a particular year. After collecting the data, he analyzed the data and prepared a report on the rainfall of the city. Using this report, he drew the following graph for a particular time period of 66 days.
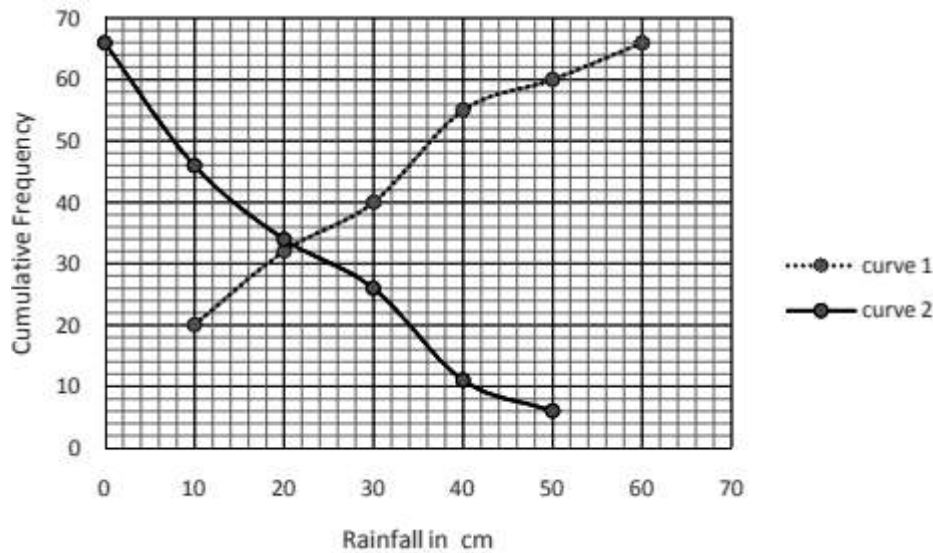


Based on the above graph, answer the following questions:

(i)  Identify less than type ogive and more than type ogive from the given graph.
(ii) Find the median rainfall of Dispur
iii)      Obtain the Mode of the data if mean rainfall is 23.4cm
iv)      Make Frequency distribution table from above graph.

34) One day, three friends Aakash, Aditya and Manoj went to Children Park to play some games.
While playing at one moment Aakash is at the point P, Aditya is at point A and Manoj is at point at B such that Aakash's distance from Aditya and Manoj are equal. If the position of Aditya and Manoj are given as (1, 2) and (3, 8) respectively and area of  triangle PAB = 10 sq. m,then find the coordinates of P. Also find the distance of Aakash from Aditya and Manoj.
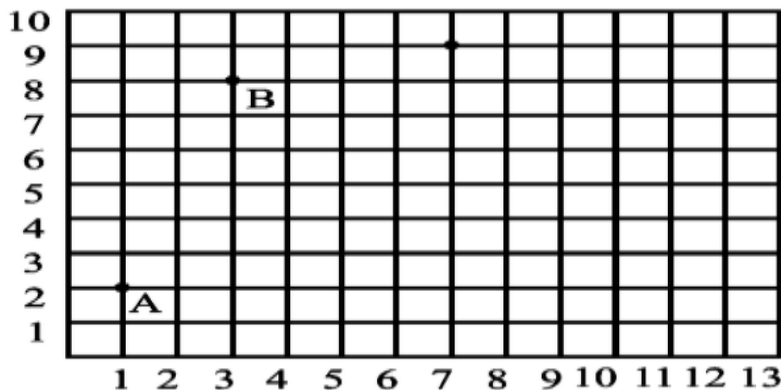
SECTION –D

35)   A man on the top of a vertical observation tower observes a car moving at a uniform speed coming directly towards it. If it takes 12 minutes for the angle of depression to change from $30^\circ$ to $45^\circ$, how soon after this will     the car reach the observation tower. Give your answer correct to nearest seconds.

36) Draw a triangle ABC with side BC = 7 cm, ∟ B = 45°, ∟ A = 105°. Then, construct a triangle whose sides are  1.6 times the corresponding sides of  ΔABC.                                                    OR
   Draw pair of tangents to circle  of radius 5 cm which are inclined at angle of 45 $^0$ .

37) A farmer connects A pipe of internal diameter 25 cm from a Canal into a cylindrical tank in his field which is 12 m in diameter and 2.5 m deep if water flows through the pipe at the rate of  3.6 km per hour in how much time will the tank be filled also find the cost of water is the canal department charges @ rupees 0.07 per metre $^3$.              OR

 A milk container is made of metal sheet in the shape of frustum of a cone whose volume is $10459\frac{3}{7}$ cm$^3$. The radii of its lower and upper circular ends are 8 cm and 20 cm respectively. Find the cost of metal sheet used in making the container  at the rate of  Rs  1.40 per square centimeter.

38) The distribution of heights in cm of 96 children is given below:

| Height | 124-128 | 128-132 | 132-136 | 136-140 | 140-144 | 144-148 | 148-152 | 152-156 | 156-160 | 160-164 |
|---|---|---|---|---|---|---|---|---|---|---|
| Children | 5 | 8 | 17 | 24 | 16 | 12 | 6 | 4 | 3 | 1 |

Draw a less than type & more than type ogive from given data ,Hence obtain median from the graph.

39 ) In an equilateral triangle ABC, D is the point on BC such that  3BD = BC , Prove that $9AD^2 = 7 AB^2$ .

40)  A train, travelling at a uniform speed for 360 km, would have taken 48 minutes less to travel the same distance if its speed were 5 km/h more. Find the original speed of the train & time taken .                          OR

i)        Solve : $\frac{1}{2a+b+2x} = \frac{1}{2a} + \frac{1}{b} + \frac{1}{2x}$

ii)         A pole has to be erected at a point on the boundary of a circular park of diameter 17 m in such a way that the differences of its distances from two diametrically opposite fixed gates A and B on the boundary is 7 metres. Find the distances from the two gates where the pole is to be erected.