

CLASS XI

SAMPLE PAPER

MATHS

[Set, Relation and Function and Mathematical Induction]

Time: - 1hr

F.M-30

(Answer ALL questions)

- 1)
- a) What is the value of $|P(P(P(\phi)))|$?
 - b) Write the smallest and largest subset of $\{1, 2, 3\}$.
 - c) $\phi \times A = ?$ Where A is any set.
 - d) Find x, y if, $(x + y, 1) = (1, x - y)$.
 - e) State with reason, which of the following are sets and which are not:
 - (i) Collection of all sets.
 - (ii) All natural numbers having at least one prime factor.
 - f) If $|A|=m$ and $|B|=n$, then find the number of relations defined from A to B?
 - g) Let $f = \{(1,3), (2,4), (3,7)\}$, $f^{-1} = \{(3,2), (4,3), (7,1)\}$. Determine $f \circ f^{-1}$ and $f^{-1} \circ f$.
 - h) Draw the graph of $y = \log_a x$ on your answer sheet where $0 < a < 1$ and write its range.
 - i) If $f(x) = \log_2 x$, then find $f^{-1}(x) = ?$
 - j) If $f\left(x + \frac{1}{x}\right) = x^2 + \frac{1}{x^2}$, $x \neq 0$, find $f(x) = ?$
- 2) Prove by method of induction that if $|A|=n$, then $|P(A)|=2^n$.
or Prove by induction that $4^{n+1} + 15n + 14$ is divisible by 9.
- 3) If $|A| = m$, $|B| = n$, then find :
 a) $|A \times B| = ?$ c) $|P(A \times B)| = ?$
 b) $|P(A) \times P(B)| = ?$
- 4) Suppose that in a class consist of a set S of 100 students, 70 of which pass in Mathematics and 60 in Physics. If no one failed in the both subjects, determine the number of students who passed in both subject?
- 5) : Let $f(x) = \sqrt{x}$ and $g(x) = x$ be two functions defined over the set of nonnegative real numbers. find $(f + g)(x)$, $(f - g)(x)$, $(fg)(x)$, and $\left(\frac{f}{g}\right)(x)$.

6) Let $A = \{1,2\}$, $B = \{1,2,3,4\}$, $C = \{5,6\}$ be sets, then verify that :

$$A \times (B \cap C) = (A \times B) \cap (A \times C)$$

7) Find the Domain and Range of the function $f(x) = \sqrt{9 - x^2}$

Ranjan Ku Mohapatra
mahapatra.ranjan@rediffmail.com
+91-9437534728